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On the convergence of Neumann series for noncompact  
operators

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## ANNOUNCEMENTS OF NEW RESULTS

(of authors having an address in Czechoslovakia)

ON THE CONVERGENCE OF NEUMANN SERIES  
FOR NONCOMPACT OPERATORS

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We consider solving of the equation

$$(1) \quad (I - T)y = x$$

by means of the Neumann series. We can show that for an element  $x$  of the Banach space  $X$  and for a bounded linear operator  $T$  on  $X$ , such that the distance of  $T$  from the subspace of all compact linear operators acting on  $X$  is less than 1, the series  $\sum T^n x$  converges to a solution  $y$  of the equation (1) if and only if  $T^n x$  converges weakly to zero as  $n \rightarrow \infty$ . This extends the earlier result of N. Suzuki (cf. [1]) dealing with a compact  $T$ .

## REFERENCES

- [1] Suzuki N., *On the convergence of Neumann series in Banach space*, Math. Ann. **220** (1976), 143-146.

AGGREGATION AND DISAGGREGATION IN MARKOV CHAINS

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*The aggregation — disaggregation method* helps to manage difficulties following from very complicated phenomena so that it enables to investigate the phenomena on two or even more hierarchical nicety levels. This method can also be used to compute the stationary distribution of the finite homogeneous Markov chain (with transition probability matrix  $P$ ).

Let us consider the following algorithm:

0. Choose an initial distribution  $p^0 > 0$ , set  $k = 0$ .
- 1.1. *Aggregation*: compute the aggregated transition probability matrix  $\bar{P}(p^k)$ .
- 1.2. *Solving the aggregated problem*: compute the aggregated stationary distribution  $\bar{p}(p^k)$  concerning the transition probability matrix  $\bar{P}(p^k)$ .
- 1.3. *Disaggregation*: compute the corrected distribution  $\tilde{p}^k$  by disaggregating the aggregated stationary distribution.
2. Perform 1 iteration step of the successive approximations method:  $p^{k+1} = \tilde{p}^k P$ .
3. *Convergence test*: if the norm  $\|p^{k+1} - p^k\|$  is sufficiently small, the computing finishes, otherwise increase  $k$  by 1 and repeat the computing from the step 1.1 ( $\|x\|_1$  can be used as the norm).

A theorem is valid for this algorithm: