Andrzej Lelek On fixations of sets in Euclidean spaces

In: (ed.): General Topology and its Relations to Modern Analysis and Algebra, Proceedings of the symposium held in Prague in September 1961. Academia Publishing House of the Czechoslovak Academy of Sciences, Prague, 1962. pp. 260.

Persistent URL: http://dml.cz/dmlcz/700918

Terms of use:

© Institute of Mathematics AS CR, 1962

Institute of Mathematics of the Academy of Sciences of the Czech Republic provides access to digitized documents strictly for personal use. Each copy of any part of this document must contain these *Terms of use*.



This paper has been digitized, optimized for electronic delivery and stamped with digital signature within the project *DML-CZ: The Czech Digital Mathematics Library* http://project.dml.cz

ON FIXATIONS OF SETS IN EUCLIDEAN SPACES

A. LELEK

Wrocław

The fixation of a collection C of sets is here understood to mean a set intersecting each element of C.

Theorem 1. If C is a collection of disjoint continua lying in a bounded subset of the plane and having diameters greater than 1, then there exists a compact fixation F of C such that dim F = 0.

Theorem 2. If C is a collection of components of a compact subset of the n-dimensional Euclidean space (where n = 2, 3, ...) and all the elements of C have diameters greater than 1, then there exists a compact fixation F of C such that dim $F \leq n - 2$.

Whether the hypothesis concerning C in theorem 2 can be replaced by one similar to the hypothesis in theorem 1, namely that C is a collection of disjoint continua lying in a bounded subset of the *n*-dimensional Euclidean space (where n = 3, 4, ...) and having diameters greater than 1, remains an open question.

The proofs of these theorems and some related results will be published in Fundamenta Mathematicae in two forthcoming papers of D. ZAREMBA and myself.